MATH 122 A, Spring 2019: Calculus 11

| INSTRUCTOR | Dr. Adam Childers | Phone: (540) 375-2449 |
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| CLASS MEETINGS | Mondays, Wednesdays, Fridays: 10:50 PM - 11:50 PM in Trexler 374 Thursdays <br>  <br>  <br> (Lab): 8:30 AM - 10:00 AM in Trexler 372 |  |

OFFICE HOURS MWF 1:10-2:20PM, Thurs 10:00-11:00AM, and by appointment.

COURSE
OBJECTIVES

INTENDED
LEARNING
OUTCOMES

REQUIRED
MATERIALS

This course provides a continuation of the study of calculus. Topics to be studied include
more applications of the definite integral, sequences and series and applications of them, and vectors and functions of one variable.

By the end of this course, successful students will be able to:

- apply the theory of differentiation and integration to model and solve real-world problems.
- recognize a differential equation and be able to both solve basic differential equations and discuss what a differential equation tells you about the process it models.
- determine the behavior of infinite series and understand the role of power series and Taylor series in modern mathematics.
- utilize vectors in two-dimensional and higher-dimensional coordinate systems to model graphs and equations, and apply methods of Calculus to these graphs and equations.
- recognize the role of technology in Calculus, understand when it should be used, and be aware of its limitations.

Textbook: Calculus: Early Transcendental Functions, by Smith and Minton, 4th Edition Lab Technology: Laptop with Mathematica installed

COMMITMENT HOURS

COURSE GRADES

This course expects you to spend at least 12 hours of work each week inside and outside of class.

The following table lists the weights for the various forms of assessment for this class.
Homework 13\% Labs \& Recitations 12\% Mastery Exams 75\%
A grade scale will be determined after final grades are computed, but will be no worse than the scale given below:

|  |  | $\mathrm{B}+$ | $87-89$ | $\mathrm{C}+$ | $77-79$ | $\mathrm{D}+$ | $67-69$ |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| A | $93-100$ | B | $83-86$ | C | $73-76$ | D | $63-66$ | F | $0-59$ |
| A- | $90-92$ | B- | $80-82$ | C- | $70-72$ | D- | $60-62$ |  |  |

READING The key to learning a topic in mathematics is participation. We will strive to have an active, rather than passive, classroom environment. Near the end of the syllabus is a day-by-day outline of the sections that will be discussed in class. You are fully expected to have read the upcoming section before the class meeting! This does not mean you need to understand everything, but rather you should be familiar with the definitions and concepts from the sections. You should also reread the section after class so that you can clarify topics from class and help prepare you further.

We will be making use of "Mastery-Based Examination," a system that is probably very different from what you are used to; do not hesitate to ask me questions in class or my office at any time. In the mathematics community many are working with and researching this technique, and one of the best starting sources for understanding can be found at https : //mbtmath. wordpress . com Much of what you'll find on this syllabus is taken from this resource.

Short Description: You only receive credit for answers that demonstrate you completely understand (have mastered) a topic. But, you get many chances to display mastery throughout the semester with no penalty at all for earlier attempts.

Long Description: The course has been boiled down to 22 essential types of questions, or "topics," and your mastery of questions on these topics is assessed through four mastery testing days, smaller mastery testing opportunities between testing days, and the final exam periods. Each problem submitted is graded as either "mastered" or "not mastered" and a grade of "mastered" indicates that you have demonstrated full understanding of the concept being tested and further work on the topic is not necessary. Once you have mastered a problem you need not ever attempt it again on a future exam, including the final exam. There is no penalty whatsoever for multiple attempts taken to achieve mastery.

Your overall exam grade is then determined by the number of topics you have mastered throughout the semester; see below for more about how the number of topics translates to a grade for the exam portion of the class and what the topics are!

Why such a different examination policy? A typical policy that has four tests on which material on test 1 is not revisited until the final exam promotes a "fixed mindset"
mentality and does not encourage growth in learning; allowing multiple attempts to achieve mastery on a single topic is a "growth mindset" - we firmly believe that you can all do this! It may just take some of you a little longer or shorter for certain topics. Rather than thinking "I can't do this" you should be thinking "I can't do this, yet" and work towards getting it done.

Notes on Mastery-Based Examination (in no specific order, credit to Austin Mohr): Clear content objectives, students continually know exactly what they need to work on to improve.

- Credit only for eventual mastery. No partial credit.
- Multiple attempts with complete forgiveness.
- A points-based system sets arbitrary deadlines by which time perfection must be attained or else penalties apply. • Perseverance:

Points: Try a problem once, maybe twice, hope for the best.
Mastery: Keep trying until you succeed (and I know you can).

- Use of feedback on exams:

Points: Do you agree with the instructor's grading?
_ Mastery: What can I do to fully demonstrate that I understand the concept (improvement!)?

- Reduced Anxiety:
_ Points: Every exam has the potential to damage your GPA.
_ Mastery: No one exam can harm your grade.
- Intelligent Test Preparation: You may actually choose to skip problems on a test. Better to achieve mastery on some than to demonstrate mediocrity on all. Given time constraints of the latter tests, most students will only be able to focus on 5-8 problems in 90 minutes. • Formative Assessment:
_ Points: How many points is this error worth?
_ Mastery: Will the student benefit from studying the concept again?
- No longer will any of us have to wonder just what exactly a $7 / 10$ means on a problem compared to an $8 / 10$.
- In most points-based systems, a blank exam question is a heavy blow to a student's grade. On the other hand, a student who provides a couple relevant formulas and something resembling the beginning of a solution may receive half credit or more. In the presence of constrained study time, a good strategy is to learn some basics about every test item. Such a student may earn half credit on most items together with a few lucky shots on easier items, which amounts to a passing grade overall. Take a moment to consider whether this experience has adequately prepared the student to apply mathematical thinking to nontrivial problems in the future.

The "broad and superficial" strategy employed above earns no credit under a masterybased system. Instead, a student who wishes to earn a passing exam grade must fully understand an appreciable subset of the main ideas of the course, and a student wishing to earn an A grade must fully understand most or all of the main ideas of the course. Even if students spend no time studying a particular item, we contend that the experience of pursuing deep understanding on the other items leaves them in a stronger position to engage deeply with the troublesome topic when it is needed in the future.

Moreover, depth of understanding is critical to one's ability to apply existing mathematical knowledge in novel domains.

There are four mastery days listed on the day-by-day schedule part of this syllabus. On these days, you will have the opportunity to attain mastery in any of the topics we have covered up to that date. There are also four mini-mastery days listed on the schedule, and on these days, we will use 30 minutes during a regular class period so that you can attempt mastery in up to two topics of your choice; you must contact the instructor prior 9 AM the day of a mini-mastery attempt with your choice of topics to attempt. Finally, you will have two opportunities during the final exam week in order to achieve mastery.

The exam portion of your course grade will be based on the number of topics mastered; here is a conversion of the number mastered to a percentage for the exam portion of the grade.


HOMEWORK

QUIZZES

A problem set will be assigned for virtually all sections that we cover; each problem set will consist of 2 required problems and a number of practice problems. Note that the required problems will not be from the textbook and will instead be posted on Inquire. The required problems will be graded for correctness and presentation ( 3 points for correctness and 2 points for presentation) for a total of 10 points. You are encouraged to do and submit as many of the practice problems as you would like, and the instructor will provide feedback on those problems. When you turn in your problem set, the 3 required problems should all be first, and in order as they appear in the textbook. Your homework should be neat, organized, and stapled!

In the spirit of mastery-based testing, these problem sets do not have a due date. However, you may not turn in or received credit for a problem set after you have received mastery for the topic or topics that correspond to that problem set. Note that you are encouraged to collaborate on problems sets, but you must write up your own solution. If you are looking at another person's work or asking someone what to do next while writing up your problem set, then you are in violation of the academic integrity policy of Roanoke College.
There may be written quizzes in this class. They may either be in-class quizzes or takehome quizzes. I may occasionally warn you about an upcoming quiz but you should be prepared to take a quiz on any given day, including lab days. These quizzes will count as a homework assignment.

We will meet in Trexler 372 every Thursday from 8:30 AM to 10:00 AM. This time will mostly be spent working in groups on various problems. Some days will be Lab days, in which you will work on interesting applications of the calculus we are studying and use Mathematica to help you in this process. Other days will be Recitation days, led by your student lab leaders, in which you will focus on working problems to help solidify concepts from class. Other Thursdays will be Mastery days, which will allow you more time than during regular class time. Lab and Recitation days are more informal and should be noisy. Ask questions of lab leaders and classmates!
(1) Be on time! (2) Bring laptop, writing utensil, paper, textbook, notes.
(3) Learn Mathematica! (4) Think! (5) Work with others!

FINAL EXAM Since this class has regular meetings during block 4 and lab time on Thursdays during block 9, we have two days on which to have our "final exam." Of course, if you have mastered all of the topics for the class (or all of the topics you wish to master), you need not show up for either final exam slot! That said, you will have the opportunity to master topics on Friday, April 26 from 8:30 ANI to 11:30 AM and on Monday, April 29 from 8:30 AM to 11:30 AM.
Attendance is critical to the understanding of the material in the course; it is both

ATTENDANCE \& MAKE-UP WORK required
and expected. Any absence that is not discussed with the instructor prior to the missed class is considered unexcused. When absent, excused or unexcused, you are responsible for all material covered in class. You will not be allowed to make up any work missed due to an unexcused absence. Should you miss a class or part of a class, email or talk to me as soon as possible to see if anything can be done to help you catch up.

MCSP
The Department of Mathematics, Computer Science and Physics offers a series of discussions that appeal to a broad range of interests related to these fields of study. These co-curricular sessions will engage the community to think about ongoing research, novel applications and other issues that face our discipline. Members of this class are invited be involved with all of these meetings; however participation in at least two of these sessions is mandatory. After attending, students will submit a one page paper reflecting on the discussion within a week of attending the talk. This should not simply be a regurgitation of the content, but rather a personal contemplation of the experience. These reaction papers will be counted as homework and should be uploaded to Inquire using the appropriate link.
Students are expected to adhere to the Academic Integrity policies of Roanoke College. All work submitted for a grade is to be your own work! No electronic devices other than calculators can be taken out during any class or testing period (this includes cell phones) unless written consent is given by the professor (e.g. Mathematica may be allowed for some tests). Note that looking at or using your cell phone during a test or quiz is considered a violation of Academic Integrity regardless of your purpose or intent in doing so.

SUBJECT TUTORING Subject Tutoring, located on the lower level of Fintel Library (Room 5), is open 4:00

PM - 9:00 PM, Sunday - Thursday. We are a Level Il Internationally Certified Training Center through the College Reading and Learning Association (CRLA). Subject Tutors are highly trained Roanoke College students who offer one-on-one tutorials in a variety of general education and major courses such as: Business, Economics, Mathematics, INQ 240, Modern Languages, Lab Sciences, INQ 250, and Social Sciences. Tutoring sessions are available in 15,30 , or 45 -minute appointments. Feel free to drop by for a quick question or make an appointment at https: subj!ct_tutoring@roar . edu //libguides . roanoke . edu/subject_tutoring for a
longer one-on-one appointment. For questions or concerns, please contact us at 540-3752590 or

| Mon | Jan 14 | 7.1 | Introduction and Differential Equations <br> Wed <br> Jan 16 |
| :--- | :--- | :--- | :--- |
|  | No Class |  |  |
| Thur | Jo Lab 17 |  |  |
| Fri |  | Na |  |
|  | Jan 18 |  | No Class |


| Fri | Apr 5 | 8.7 | Applications of Taylor Series |
| :--- | :--- | :--- | :--- |


| Mon | Apr 8 | 8.8 | Applications of Taylor Series and Mini-Nlastery <br> Wed <br> Apr 10 |
| :--- | :--- | :--- | :--- |
| In-Class Lab: Hidden Figures    <br> Thur Apr 11 8.9 Recitation <br> Fourier Series <br> Fri Apr 12  Fourier Series <br> Review <br> Mon Apr 15 8.9 Mastery Day <br> Wed <br> Apr 17 <br> No Class: Good Friday    <br> Thur Apr 18  Exam Block 8:30 AM - 11:30 AIVI: Mastery <br> Fri <br> Apr 19 <br> Fri Apr 26 Exam Block 2:00 PM - 5:00 PM: Mastery   <br> Mon Apr 30  Day |  |  |  |

TOPICS

| Topic Number | Name | Rough Textbook <br> Alignment |
| :---: | :---: | :---: |
| 1 | Differential Equations: Modeling | 7.1 |
| 2 | Differential Equations: Solving | 7.2 |
| 3 | Projectile Motion: Basic | 5.5 |
| 4 | Integration: Physics | 5.6 |
| 5 | Integration: Probability | 5.7 |
| 6 | Vectors: Calculations, Basic | 10.1, 10.2 |
| 7 | Vectors: Calculations, Advanced | 10.3, 10.4 |
| 8 | Vectors: Applications | 10.3, 10.4 |
| 9 | Lines and Planes in Space | 10.5 |
| 10 | Vector-Valued Functions: Basic | 11.1 |
| 11 | Vector-Valued Functions: Calculus | 11.12 |
| 12 | Projectile Motion: Advanced | 11.3 |
| 13 | Polar Coordinates |  |
| 14 | Parametric Equations | 9.1, 9.2 |
| 15 | Sequences | 8.1 |
| 16 | Series: Core | 8.2 |
| 17 | Series: Ratio Test | 8.5 |
| 18 | Power Series | 8.6 |
| 19 | Taylor Series: Core | 8.7 |
| 20 | Taylor Series: Error | 8.7 |
| 21 | Taylor Series: Applications | 8.8 |
| 22 | Fourier Series | 8.9 |

